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SOME SEQUENTIAL SELECTION PROCEDURES FOR GOOD REGRESSION MODELS.

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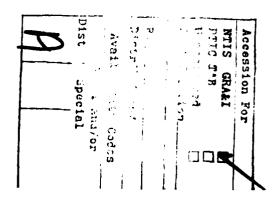
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ABSTRACT

In the past decade a number of fixed sampling methods have been developed for selecting the "best" or at least a "good" subset of variable in regression analysis. We are interested in deriving a sequential selection procedure to select a subset of a random size including all good regression equations. Tables for an example are given at the end of this paper.

1. INTRODUCTION

In the past decade a number of fixed sampling methods have been developed for selecting the "best" or at least a "good" subset of variables in regression analysis (see e.g. Arvesen and McCabe (1975) and Spjøtvøll (1972)). In this paper, we are interested in deriving a sequential selection procedure to select a random size subset including all "good" regression equations.



Tables for an example are given at the end of this paper.

2. SEQUENTIAL SUBSET SELECTION PROCEDURE

Before discussing the regression problem, we develop general results applicable to the selection of "good" or "superior" populations defined later.

Let π_0 , π_1 ,..., π_k denote k+1 normal populations with unknown means μ_0 , μ_1 ,..., μ_k and variances σ_0^2 , σ_1^2 ,..., σ_k^2 . Assume that σ_0^2 is known but σ_i^2 (1 \leq i \leq k) are unknown. Let the ranked

values of σ_i^2 be denoted by $\sigma_{[1]}^2 \leq \ldots \leq \sigma_{[k]}^2$. We wish to derive a method to construct a sequential procedure to select a subset containing all "superior" populations - the populations with smaller variances, with a probability not less than P*, (0 < P* < 1), a specified constant. We assume that $\sigma_0^2 = 1$.

Let X_{in} denote the nth observation from population π_i . It is assumed that the observations X_{i1},\ldots,X_{in} are independent random variables. Define

$$\bar{X}_{in} = \frac{1}{n} \sum_{j=1}^{n} X_{ij}$$

and

$$s_{in}^2 = \frac{1}{n-1} \sum_{i=1}^{n} (X_{ij} - \bar{X}_{in})^2$$
.

The selection procedure will depend upon $\{s_{in}^2\}$ which is a sufficient and transitive sequence and also invariantly sufficient for $\{\sigma_i^2\}$.

A population π_i is said to be "superior" (or "good") if $\sigma_i^2 \leq \Delta$, to be "inferior" (or "bad") if $\sigma_i^2 > \Delta$, where Δ is a specified constant greater than 1. Let Ω be the parameter space which is the collection of all possible parameter vectors $\underline{\alpha} = (\sigma_1^2, \ldots, \sigma_k^2)$. Let t denote the unknown number of inferior

populations in the given collection of k populations. We have $0 < t \leq k$. Let

$$\omega_{\mathbf{t}} = \{ \underline{\theta} \mid \sigma_{[1]}^2 \leq \dots \leq \sigma_{[k+t]}^2 \leq \Lambda < \sigma_{[k-t+1]}^2 \leq \dots \leq \sigma_{[k]}^2 \}.$$
Then $\Omega = \bigcup_{\mathbf{t}=0}^{k} \Omega_{\mathbf{t}}$.

For the subset selection procedure R, two constants Δ and P* with $\Delta > 1$, 1 > P* > 0, are specified and we wish to select a subset containing all superior populations with a probability of at least P*. When all the superior populations are contained in the selected subset, we say a correct decision (CD) has been made. Thus we require a procedure for which

$$P_{\theta}(CD|R) \ge P^*$$

for all $g \in \Omega$.

Let $g_{\sigma_i^2}(s_{in}^2)$ denote the probability density of s_{in}^2 depend-

ing on the parameter σ_{i}^{2} . We define the log-likelihood ratios

$$\ell_n(s_{in}^2) = \log g_{\Lambda}(s_{in}^2) - \log g_{1}(s_{in}^2)$$
 (2.1)

upon which the procedure is based.

Elimination type sequential selection procedure R for selecting the superior populations.

Begin by taking n_1 (\geq 1) independent observations from each of the k populations. Calculate the values of the k log-likelihood ratios ℓ_{n_1} ($s_{in_1}^2$), $1 \leq i \leq k$. For any i, if

$$\ell_{n_1}(s_{in_1}^2) \geq a$$
,

where a = $\log(k(k+1)/2(1-P^*))$, we eliminate the population π_i from further consideration. We proceed to the next (second) stage by taking $n_2 - n_1$ independent observations on each of the remaining populations. The log-likelihood ratios for the contending populations are again computed and the same elimination rule is used

except that $\ell_{n_2}(s_{in_2}^2)$ everywhere replaces $\ell_{n_1}(s_{in_1}^2)$. We continue

in this manner until the elimination is stopped, at which time the procedure is terminated with the declaration that the remaining populations are the superior populations. If after applying this rule at the sth stage (say), the number of remaining populations is zero, then we select the population π_0 which is the control population.

Note that n_1 is the sample size of that stage of the procedure at which a decision may be made, for the first time, to reject one or more populations. Let $n_2 > n_1$ be the sample size of the next stage of the procedure at which such a decision may be made, and in general let $n_s > n_{s-1}$ be the sample size of the stage of the procedure at which the sth decision to reject one or more populations may be made. Let N be the stage at which the procedure terminates. It is clear that if there are k populations to start with, then N $\leq n_k$ (see Gupta and Huang (1975)).

We assume that

$$P_{2i}(s_{in}^2) \ge a \quad \text{for some n}$$
 (2.2)

is a nondecreasing function of σ_i^2 . A sufficient condition for this is discussed by Hoel (1970). Without loss of generality, we assume that π_1,\ldots,π_{k-1} are the superior populations. Since the procedure R is truncated, we have

3. APPLICATIONS TO SELECTION OF "GOOD" OR "SUPERIOR" REGRESSION EQUATIONS

Assume the following standard linear model as follows,

$$Y = X\beta + \varepsilon \tag{3.1}$$

where X is an nxp known matrix of rank p \leq n, β is a pxl parameter vector, and ϵ \sim N(0, $\sigma_0^2 I_n$). Consider the models for any r, $2 \leq r \leq p-1$,

$$Y = X_{ri}\beta_{ri} + \epsilon_{ri} \tag{3.2}$$

where X_{ri} is an nxr matrix of rank r with $X_{11}^1 = [1, \ldots, 1]_{1Xn}$, β_{ri} is a rxl parameter vector, and $\varepsilon_{ri} - N(0, \sigma_{ri}^2 I_n)$, where $i=1, \ldots, k_r = \binom{p-1}{r-1}$. Let $k = \sum_{r=2}^{p-1} k_r$. The goal is to include all the designs X_{ri} (or sets of independent variables) associated with $\sigma_{[j]}^2$, $j=1, \ldots, k-t$.

Note that for any r, $2 \le r \le p-1$, if

$$SS_{ri} = Y'\{1 - X_{ri}(X_{ri}'X_{ri})^{-1}X_{ri}'\}Y = Y'Q_{ri}Y,$$

then following Searle (1972, p. 57)

$$SS_{ri}/\sigma_0^2 + \chi^2 \{v_r, (X\beta)'Q_{ri}(X\beta)/(2\sigma_0^2)\},$$

where v_r = n-r, for $1 \le i \le k_r$. Note that the noncentrality parameter is not zero in general and that

$$\sigma_{ri}^2 = \sigma_0^2 + (\chi_\beta)'Q_{ri}(\chi_\beta)/v_r.$$

If σ_0^2 is not equal to 1, then we consider the linear model $Y/\sigma_0 = X_B/\sigma_0 + E'$, $E' = N(0,I_n)$. Thus we assume without loss of generality that $\sigma_0^2 = 1$.

We know that the non-central $\chi^2(x,\lambda)$ with non-centrality parameter λ has monotone likelihood ratio in x. Hence the monotonicity of (2.2) is satisfied. We can apply the sequential procedure R to select superior regression equations by replacing $s_{\rm ri}^2$, by $SS_{\rm ri}/v_{\rm r}$.

4. COMPUTATION OF (2.1)

Let $U_{ri} = SS_{ri}/v_r$. The probability density of U_{ri} is

$$g_{2}(U_{ri}) = v_{r} \left[e^{-\lambda} \int_{k=0}^{\infty} \frac{\lambda^{k}(v_{r}U_{ri}) - \frac{1}{2}(v_{r}U_{ri})}{\sum_{k=0}^{1} \frac{1}{2}v_{r} + k} \int_{r(\frac{1}{2}v_{r} + \kappa)} \frac{\lambda^{k}(v_{r}U_{ri}) - \frac{1}{2}v_{r} + \kappa}{\sum_{k=0}^{1} \frac{1}{2}v_{r} + \kappa} \right]$$

where $\sigma_{ri}^2 = 1 + (XB)'Q_{ri}(XB)/v_r$, $v_r = n-r$ and $\lambda = (XB)'Q_{ri}(XB)/2$. If $\sigma_{ri}^2 = 1$, then $\lambda = 0$ and if $\sigma_{ri}^2 = \Delta$, then $\lambda = (\Delta-1)v_r/2$. Hence

$$q_{\lambda}(U_{ri})/q_{1}(U_{ri}) = e^{-\lambda} \sum_{k=0}^{\infty} \frac{\lambda^{k}}{k!} \left[\frac{v_{r}U_{ri}}{2} \right] \frac{k - r(\frac{1}{2}v_{r})}{r(\frac{1}{2}v_{r} + k)}$$
 (4.1)

where $\gamma = (\Lambda-1)v_{r}/2$. Let

$$a_k = \frac{e^{-\lambda} k}{k!} \left[\frac{v_r U_{ri}}{2} \right]^k \frac{\Gamma(\frac{1}{2} v_r)}{\Gamma(\frac{1}{2} v_r + k)}, \quad k = 0, 1, 2, ...$$

Since

$$\frac{a_{k+1}}{a_k} = \frac{\lambda}{k+1} \left[\frac{v_r v_{ri}}{2} \right] \frac{1}{\left(\frac{1}{2} v_r + k\right)} \rightarrow 0 \quad \text{as } -k \rightarrow -\infty, \dots$$

then for any $0 < \delta < 1$, there exists q such that

$$\frac{a_{k+1}}{a_k} < \delta < 1$$
, for all $k \ge q$.

Let us consider the error due to the truncation of the series in (4.1). Let q be the number of terms in the truncated series. Then the error due to truncation of the series in (4.1) is given by

$$\sum_{k=0}^{\infty} a_{q+k} = \frac{1-6}{1-6}.$$

Given $\eta > 0$, let k_0 be the smallest positive integer k such that

$$\frac{a_k}{n} < 1$$
 and $\frac{a_{k+1}}{a_k} + \frac{a_k}{n} \le 1$.

For this k_0 , it is easy to prove that

$$0 < g_{\Lambda}(U_{ri})/g_{1}(U_{ri}) - \begin{bmatrix} k_{0}^{-1} \\ \sum_{k=0}^{\infty} a_{k} \end{bmatrix} = \sum_{k=0}^{\infty} a_{k_{0}^{+k}} \leq n.$$

Thus $g_{\Lambda}(U_{ri})/g_{1}(U_{ri})$. $\sum\limits_{k=0}^{k_{0}-1}a_{k}$ with error less than n. To evaluate $g_{\Lambda}(U_{ri})/g_{1}(U_{ri})$, the computation is very efficient.

5. EXAMPLE

In this section we present an example which will serve to illustrate the sequential subset selection procedure. The data set is taken from Neter and Wasserman (1974, p. 373), who used it to illustrate several methods of finding a "best" set of independent variables.

There are n = 55 observations on p = 5 independent variables. Then $k=2^4-2=14$. For the subset selection procedure R, two constants Δ and P* with $\Delta>1$, 1>P*>0, are specified and we wish to select a subset containing all superior regression equations with probability at least P*.

Begin by taking $n_1 (\ge 5)$ independent observations. Calculate the values of the k ratios $g_{\Lambda}(U_{ri})/g_{l}(U_{ri})$ with error n (specified). For any r, i, If

$$g_{\Lambda}(U_{ri})/g_{l}(U_{ri}) \geq b$$

where $b = k(k+1)/2(1-P^*)$, we eliminate the regression equation from further consideration. We proceed to the second stage by taking $n_2 - n_1$ independent observations on each of the remaining regression equations. The ratios are again computed and the same

| | | x ₅ | • | 3.125 | 1.571 | 5.323 | 10.731 | 11.769 | 15.9 | 16 | 6.588 | 5.207 | 4.36 | 3.61 | 6.222 | 1.615 | 1.697 | 1.611 | | | 5.152 | | | | | | | | | |
|---------|-------------|---------------------------------------|-------|--------|-------|-------|----------|--------|-------|-------|----------|-------|------------|-----------|-------|-------|------------|-------|-------|-----|-------|-------|------------|-------|-------|-------|-------|------------|------------|--------|
| | | × | 70 | 20 | 20 | 80 | 80 | 06 | 96 | 06 | 30 | 20 | 20 | 20 | 20 | 30 | ೫ | 40 | 20 | 09 | 20 | 20 | 40 | 20 | 40 | 8 | 09 | 70 | 40 | |
| | | ×3 | 21 | 24 | 7 | 31 | 56 | 56 | ೫ | 23 | 34 | 53 | 25 | 4] | 92 | 13 | 33 | 18 | 37 | 47 | 33 | 27 | 33 | 6 | 20 | 15 | 58 | 56 | 4 | |
| | tory | x ₂ | 67 | 75 | = | 165 | 279 | 306 | 477 | 368 | 224 | 151 | 109 | 148 | 112 | 21 | 99 | 59 | 72 | 201 | 170 | 140 | 69 | 79 | 29 | 125 | 583 | 83 | 81 | |
| | t Inventory | × | _ | | _ | _ | _ | | | | , | _ | , - | _ | _ | _ | _ | _ | _ | _ | | _ | | _ | _ | _ | _ | - - | , | |
| TABLE I | the Forest | >- | 82 | 112 | 24 | 185 | 301 | 284 | 467 | 410 | 279 | 182 | 126 | 160 | 141 | 31 | 78 | 45 | 93 | 220 | 207 | 170 | 95 | 66 | 82 | 136 | 653 | | 22 | |
| | Data for t | × | 3.617 | 10.333 | 5.038 | 4.368 | 6.079 | 2.333 | 2.963 | 3.957 | 5.507 | 10.24 | 7.643 | 3.512 | 2.588 | 2.867 | 2.897 | 4.596 | 6.333 | 2.5 | 7.78 | 1.968 | 6.667 | 5.311 | 7.412 | 9.414 | 4.882 | 2.739 | 1.935 | 4.769 |
| | | Х | 20 | 70 | 20 | 20 | 70 | 23 | 20 | 20 | 90 | 90 | 96 | 30 | 30 | 30 | 30 | 70 | 96 | 30 | 70 | 20 | 30 | 06 | 8 | 70 | 8 | 20 | 20 | 20 |
| | | × | 47 | 30 | 56 | 19 | 38 | σ | 27 | 23 | 29 | 52 | 42 | 33 | 34 | 9 | 59 | 55 | 5] | 38 | 20 | 31 | 9 | 45 | 17 | 59 | 71 | 23 | <u>ج</u> ز | Q Q |
| | | , , , , , , , , , , , , , , , , , , , | 170 | 310 | 131 | 83 | 231 | 21 | SS | 15 | 369 | 526 | 321 | 104 | 88 | 98 | 84 | 239 | 323 | 45 | 389 | [9 | 58 | 239 | 126 | 273 | 83 | 63 | 99 | 310 |
| | | x ₁ | | - | , | ~ | , | | | _ | , | _ | _ | ,_ | | | - - | _ | _ | _ | - | _ | , - | _ | | _ | _ | | , | |
| | | } | 200 | 358 | 167 | | 290 | 36 | 133 | 135 | 399 | 279 | 280 | 146 | 123 | 122 | 103 | 264 | 360 | 52 | 451 | 83 | 98 | 262 | 147 | 287 | 73 | 8 | 104 | 330 |

elimination rule is used. We continue in this manner until the elimination is stopped, at which time the procedure is terminated with the declaration that the remaining regression equations are the superior regression equations.

Let η = 0.1. For the value of $g_{\Delta}(U_{ri})/g_{l}(U_{ri})$, this error of η = 0.1 is small enough with respect to constant b. Table II-VII are the subsets of independent variables of elimination for the sequential subset selection procedure R.

Table III, we consider $\Delta=1.2$. If $P^*=0.9$, then the procedure R eliminates (X_1, X_5) , (X_1, X_4) and (X_1, X_3) at stage 1 $(n_1=11)$; eliminate (X_1, X_4, X_5) at stage 2 $(n_2=16)$ and eliminate (X_1, X_3, X_4) at stage 3 $(n_3=21)$. No subset is eliminated at stage 4 $(n_4=26)$. Thus the procedure is terminated. (X_1, X_2) , (X_1, X_2, X_3) , (X_1, X_2, X_4) , (X_1, X_2, X_5) , (X_1, X_3, X_5) , (X_1, X_2, X_3, X_4) , (X_1, X_2, X_3, X_5) , (X_1, X_2, X_4, X_5) and (X_1, X_3, X_4, X_5) are the set of variables of superior regression equations. We can use C_p statistic to select one of good regression equations among the set of superior regression equations. For this example, (X_1, X_2, X_4) is the set of variable of a good regression equation (cf. Neter and Wasserman (1974)). Table II-VII represents the results for $\Delta=1.1$, 1.2, 1.5, 2, 3 and 5; $P^*=0.7$, 0.8 and 0.9.

TABLE II $n = 0.1, \Delta = 1.1.$

| p* | 16 | 21 | 26 | 31 |
|-----|----------------------|--------------------------|--------------|--------------|
| 0.7 | (1.4),(1,3) (1,5) | (1,4,5),(1,3.4) | no rejection | |
| 0.8 | (1,5),(1,3) | (1,4.5),(1,3,4) (1,4) | no rejection | |
| 0.9 | (1,5),(1,3) | (1,4,5),(1.4) | (1,3,4) | no rejection |

TABLE III $\eta = 0.1$, $\Delta = 1.2$.

| p* n | 11 | 16 | 21 | 26 |
|------|------------------------------|--------------|---------|--------------|
| 0.7 | (1,4,5),(1,5) (1,4),(1,3) | no rejection | | |
| 0.8 | (1,4,5),(1,5) (1,4),(1,3) | no rejection | | |
| 0.9 | (1,5),(1,4) (1,3) | (1,4,5) | (1,3,4) | no rejection |

TABLE IV

$$r_1 = 0.1, \Delta = 1.5.$$

| p* 11 | 6 | 11 | 16 |
|-------|-------------|--------------------------------|--------------|
| 0.7 | (1,4),(1,3) | (1,4,5),(1,5) (1,3,4) | no rejection |
| 0.8 | (1,3) | (1,4,5),(1,5) (1,3,4),(1,4) | no rejection |
| 0.9 | (1,3) | (1,4,5),(1,5) (1,3,4),(1,4) | no rejection |

TABLE V

$$η = 0.1, Δ = 2.$$

| p* n | 6 | 11 | 16 |
|------|-------------------------------------|-----------------|--------------|
| 0.7 | (1,4,5),(1,5) | (1,3,4) | no rejection |
| 8.0 | (1,4),(1,3) (1,5),(1,4) (1,3) | (1,4,5),(1,3,4) | no rejection |
| 0.9 | (1,5),(1,4) (1,3) | (1,4,5),(1,3,4) | no rejection |

TABLE VI

$$\eta = 0.1$$
, $\Delta = 3$.

| n p* | 6 | 11 | 16 |
|---------|--------------------------------------|--------------|--------------|
| 0.7 | (1,4,5),(1,5),(1,3,4) (1,4),(1,3) | no rejection | |
| 0.8 | (1,4,5),(1,5) (1,4),(1,3) | (1,3,4) | no rejection |
| 0.9 | (1,4,5),(1,5) (1,4),(1,3) | (1,3,4) | no rejection |

TABLE VII

$$n = 0.1, \Lambda = 5.$$

| p* | 6 | 11 |
|-----|--------------------------------------|--------------|
| 0.7 | (1,4,5),(1,5),(1,3,4) (1,4),(1,3) | no rejection |
| 0.8 | (1,4,5),(1,5),(1,3,4) (1,4),(1,3) | no rejection |
| 0.9 | (1,4,5),(1,5),(1,3,4) (1,4),(1,3) | no rejection |

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